

# *Higgs Bosons and b Quarks*

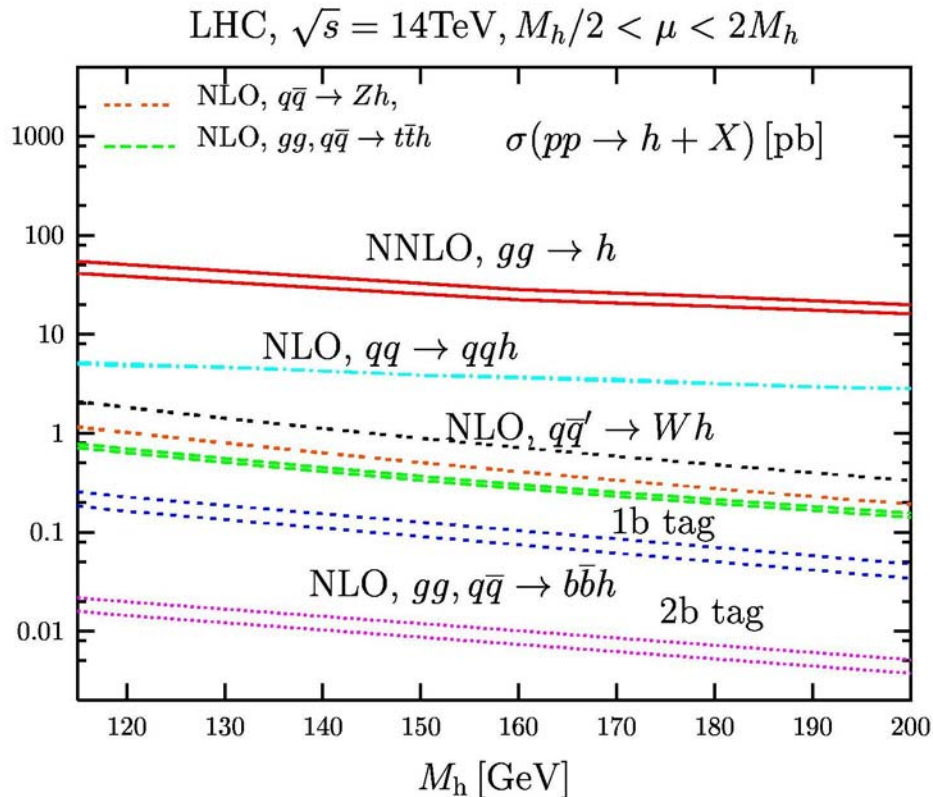
MCTP Higgs Workshop

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Chung Kao, Yili Wang, Prewit Jaiswal

# SM Production Mechanisms at LHC

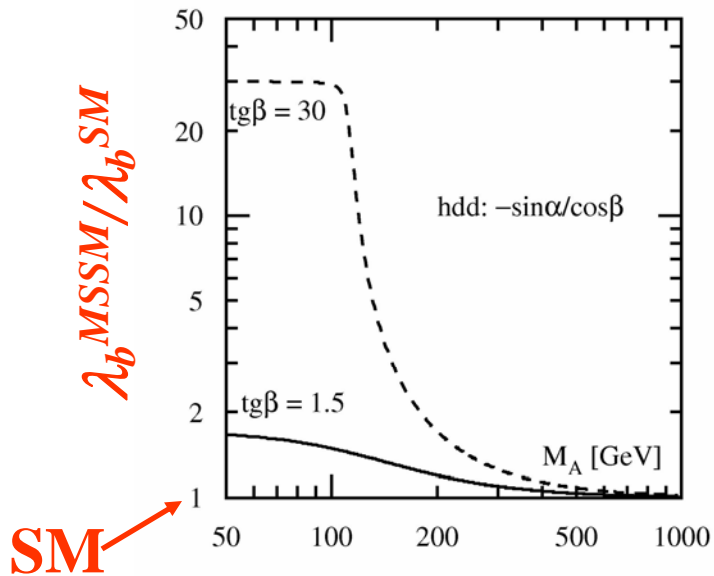


Production with b's  
very small in SM

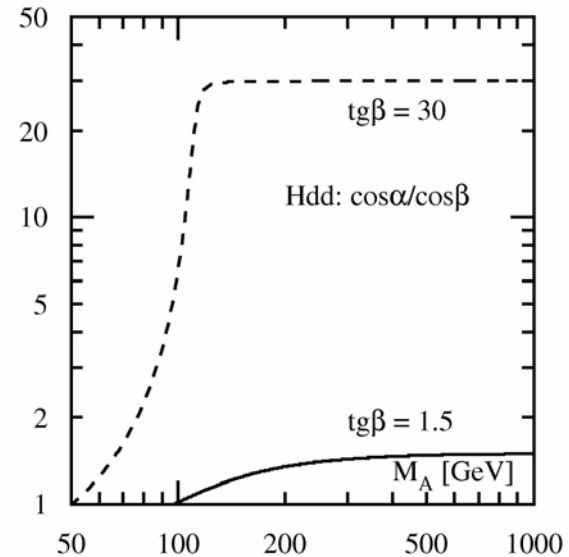
- Information about  $b\bar{b}H$  coupling must come from decays
- Progress in extracting  $H \rightarrow b\bar{b}$  from boosted Higgs techniques [Plehn]

# Higgs Couplings Very Different in MSSM

## Light Higgs



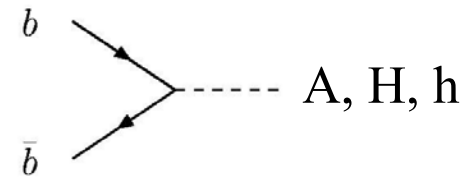
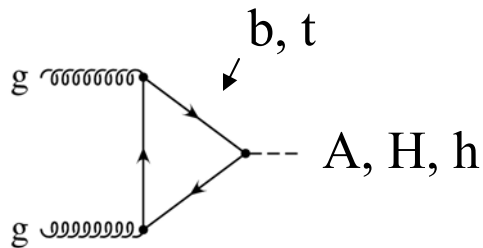
## Heavy Higgs



H, A couplings to d, s, b enhanced at large  $\tan\beta$

h couplings to d, s, b enhanced at large  $\tan\beta$  for small  $M_A$

# Relative Importance of Production Modes



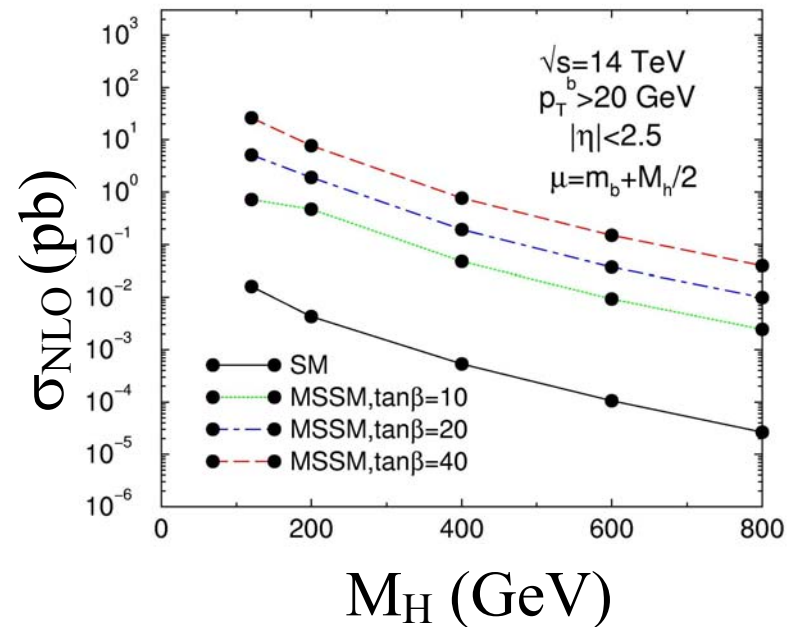
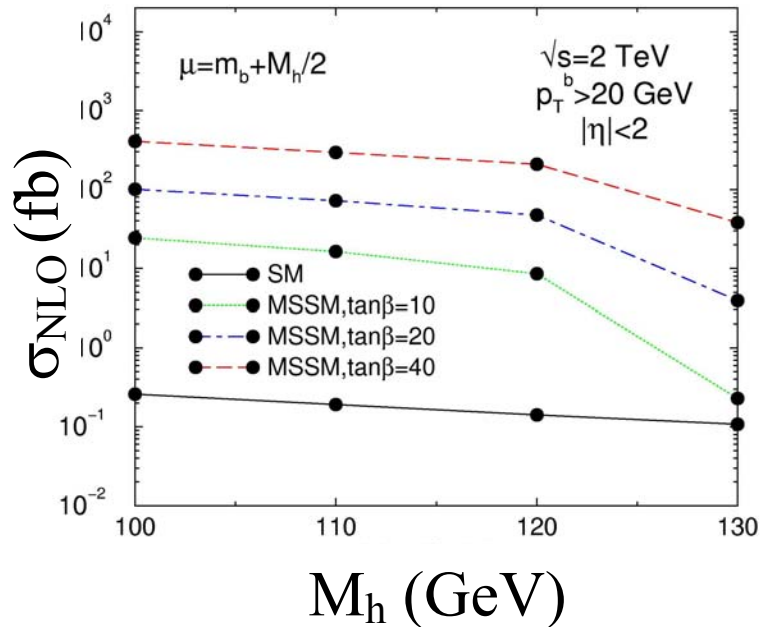
$$\sigma_{gg} = \frac{1}{M_h^2} \left( c_1 \cot^2 \beta + c_2 \frac{m_b^2}{M_h^2} + c_3 \frac{m_b^4}{M_h^4} \tan^2 \beta \right)$$

$$\sigma_{bb} = \frac{m_b^2}{M_h^4} c_4 \tan^2 \beta$$

$\Rightarrow$  At some  $\tan \beta$ , the rates for  $b\bar{b} \rightarrow A, H, h$  will be larger than those for  $gg \rightarrow A, H, h$

# $pp, p\bar{p} \rightarrow b\bar{b}H$

Rates large even at relatively small  $\tan\beta$



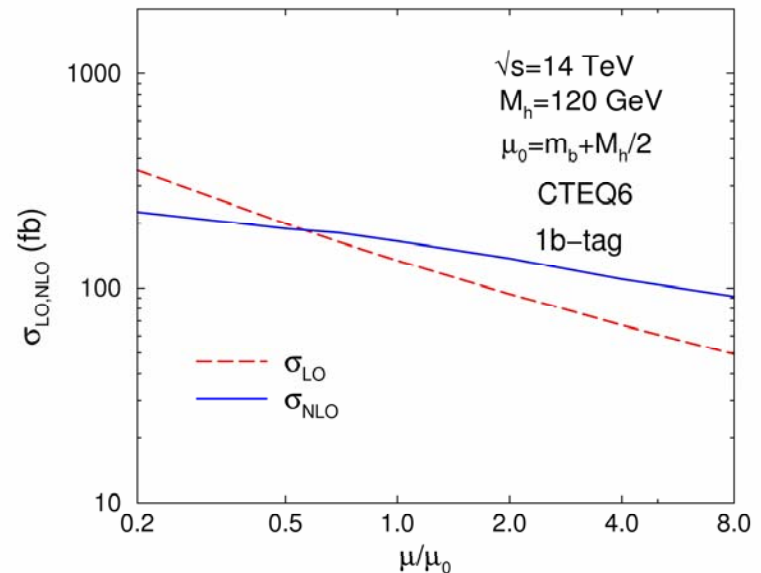
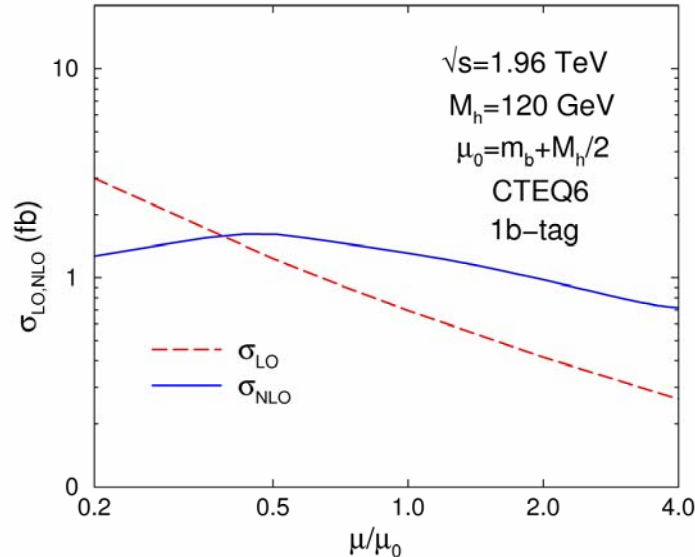
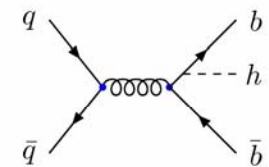
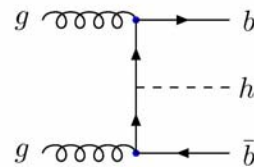
$\alpha_{\text{eff}}$  from FeynHiggs with  $M_{\text{SUSY}}=M_g = \mu=M_2=1$  TeV,  $A_b=A_t=25$  GeV

# QCD Corrections Important

- NLO corrections improve scale dependence
- NLO QCD corrections large (can't neglect them!)

• In 4 flavor number scheme:

\* Corrections don't exist in public code



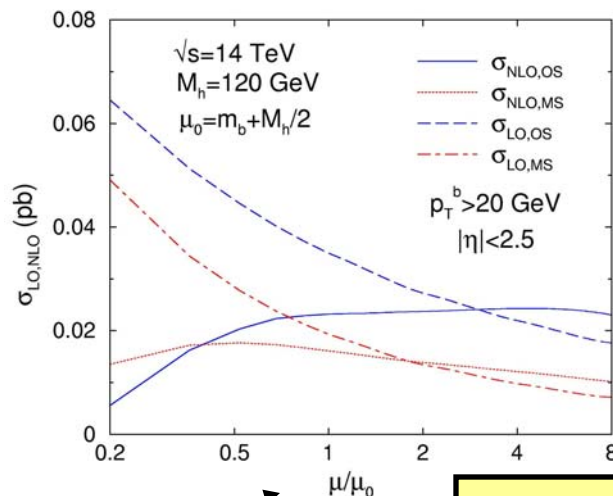
Dawson, Jackson, Reina, Wackerroth, hep-ph/0408077,0508293

Dittmaier, Kramer, Spira, hep-ph/0309204

# Residual Scheme Dependence at NLO

- Cross section proportional to b Yukawa,  $\lambda_b^2 \approx \left( \frac{m_b^2}{v^2} \right)$ 
  - $\overline{\text{MS}}$  vs on-shell definitions of b quark mass
  - $\overline{\text{MS}}$  mass depends on physical scale:  $\bar{m}_b(\mu) = m_b \left[ 1 - \frac{\alpha_s}{3\pi} \left( 4 + 3 \ln \left\{ \frac{\mu^2}{m_b^2} \right\} \right) \right]$
  - Difference between schemes is  $O(\alpha_s^4)$

$$pp \rightarrow b\bar{b}h$$



Renormalization scheme dependence

Scale dependence

- Large scheme dependence at NLO
- Effect  $\approx 10\text{-}20\%$

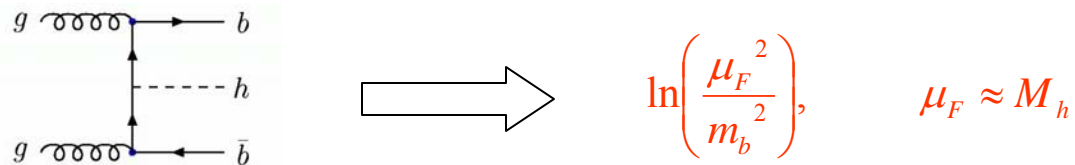
# Theoretical Issues in $b\bar{b}h$ production

Reduced  
 ↓  
 Background

- Inclusive mode: No tagged  $b$ 's
- Semi-inclusive mode: At least one tagged  $b$
- Exclusive mode: Two tagged  $b$ 's

Larger  
 ↑  
 Signal

- Treating  $b$  quarks inclusively leads to large collinear logarithms from integration over phase space



- Expansion parameter becomes  $\alpha_s \log(m_b/M_h)$



## Two Schemes for PDFs

- 4 flavor number scheme (Fixed Flavor Number Scheme)
  - No b quarks in initial state
  - Lowest order process involving Higgs and b's is  $gg \rightarrow b\bar{b}h$
  - No kinematic approximations
- 5 flavor number scheme (Variable Flavor Number Scheme)
  - Define b quark PDFs (absorbs large logarithms)

$$b(x, \mu) = \frac{\alpha_s}{2\pi} \ln\left(\frac{\mu^2}{m_b^2}\right) \int_x^1 \frac{dz}{z} P_{bg}\left(\frac{x}{z}\right) g(z, \mu)$$

- Higgs produced with no  $p_T$  at lowest order ( $b\bar{b} \rightarrow h$ )
- Higgs  $p_T$  generated at higher orders in expansion
- Both CTEQ and MSTW use this scheme for PDFs

# Re-ordering of Perturbation Theory

- 0 b tag process in 5FNS:

$$\Lambda_b = \log(M_h^2/m_b^2)$$

- LO:  $b\bar{b} \rightarrow h$   $O(\alpha_s^2 \Lambda_b^2)$
- NLO: Virtual + real corrections  $O(\alpha_s^3 \Lambda_b^2)$
- NLO:  $bg \rightarrow bh$   $O(\alpha_s^2 \Lambda_b)$ , correction of  $O(1/\Lambda_b)$
- NNLO:  $gg \rightarrow b\bar{b}h$   $O(\alpha_s^2)$ , correction of  $O(1/\Lambda_b^2)$

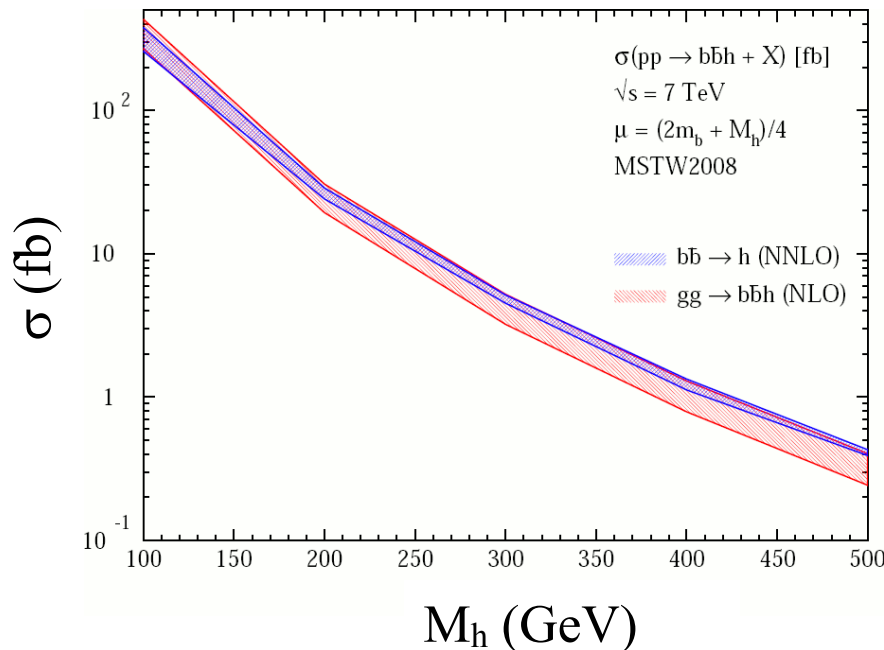
- 1 b tag process in 5FNS:

- LO process is  $bg \rightarrow bh$ : Tree level,  $O(\alpha_s^2 \Lambda_b)$
- NLO includes new subprocess:  $gg \rightarrow b\bar{b}h$ ,  $O(1/\Lambda_b)$  correction

4FNS and 5FNS must agree at high enough order in perturbation theory

# Inclusive Cross Section for $b\bar{b} \rightarrow h$ : 0 b tags

$b\bar{b} \rightarrow h$  vs  $gg \rightarrow b\bar{b}h$



4FNS: NLO QCD

5FNS: NNLO QCD

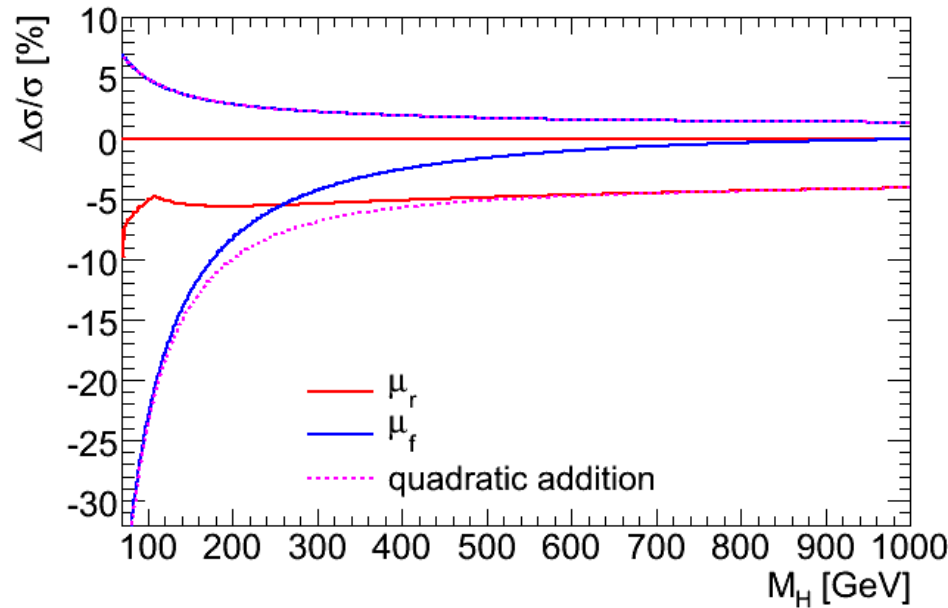
Agreement best at low  $M_h$

S-ACOT Scheme:  $\sigma_{tot} \approx \sigma_{bb} + \sigma_{sub} + \sigma_{gg}$

$\sigma_{sub}$  takes care of double counting from  $g \rightarrow b\bar{b}$

# Issues with Factorization Scale Dependence?

5FNS,  $b\bar{b} \rightarrow h$  @NNLO,  
MSTW2008,  $\sqrt{s}=7$  TeV

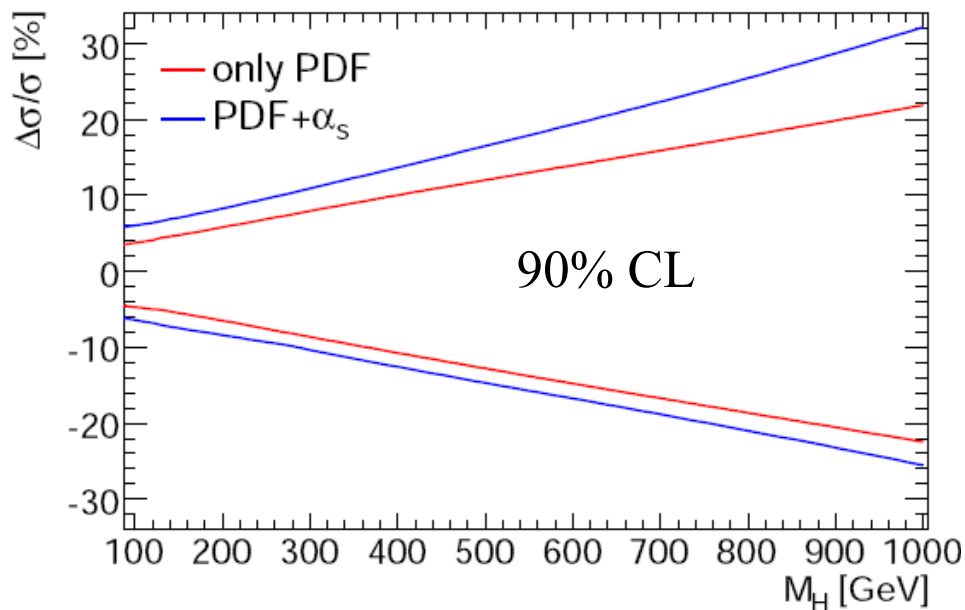


$$0.2M_H < \mu_R < 5M_H$$

$$0.1M_H < \mu_F < 0.7M_H$$

# PDF uncertainty for $b\bar{b}\rightarrow h$

5FNS,  $b\bar{b}\rightarrow h$  @NNLO,  
MSTW2008,  $\sqrt{s}=7$  TeV



Large PDF  
uncertainty for  
heavy Higgs!

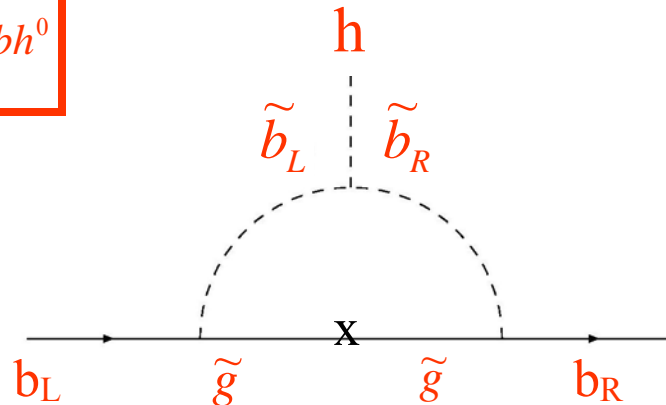
# SUSY QCD / Electroweak Corrections

- Compute in effective Lagrangian approach

$$L_{eff} = \frac{\bar{m}_b(\mu)}{v_{SM}} \left( -\frac{\sin \alpha}{\cos \beta} \right) (1 + \delta_{SQCD} + \delta_{EW}) \bar{b} b h^0$$

- SUSY QCD:

$$\delta_{SQCD} \equiv \left( \frac{1}{1 + \Delta m_b} \right) \left( 1 - \frac{\Delta m_b}{\tan \beta \tan \alpha} \right)$$



- Similarly for weak effects:  $\delta_{EW} \sim 2-4\%$

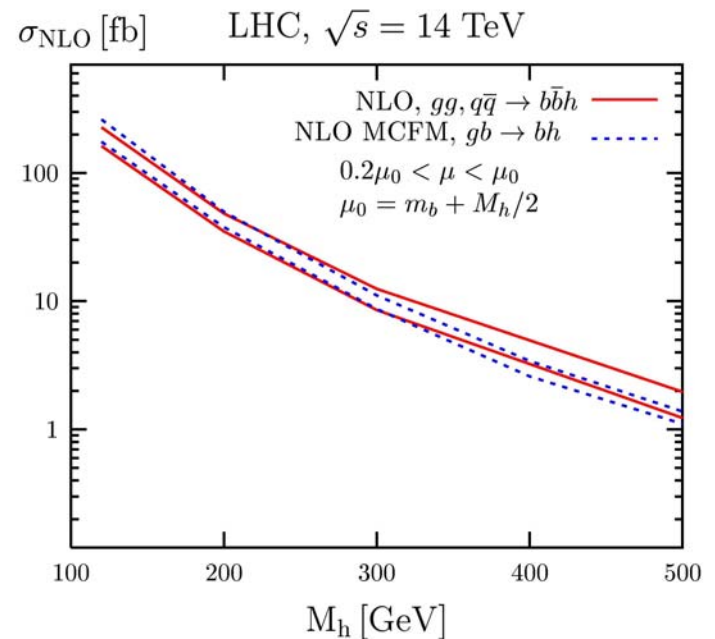
Effective Lagrangian approach works to 1-3% for  $b\bar{b} \rightarrow h$  for SQCD and EW effects

## Bottom Line: Inclusive 0 b Tag

- Calculate SM in 5FNS to NNLO (using bbh@NNLO)
  - Find MSSM couplings from HDECAY or FeynHiggs
- $\mu_R$  uncertainty  $\sim 5\%$
- $\mu_F$  uncertainty  $\sim 5\%$  for  $M_H > 200$  GeV, up to 20% for lighter  $M_H$
- Scheme dependence  $\sim 10\text{-}20\%$
- PDF uncertainty  $\sim 10\text{-}20\%$
- SQCD and EW effects accurately included using effective Lagrangian approach ( $\Delta m_b$ )
  - These may be large

# Easier experimentally: bH production

- 4 flavor number scheme
  - NLO QCD
- 5 flavor number scheme
  - NLO QCD [MCFM with top triangle removed]
  - SUSY QCD corrections
  - EW corrections

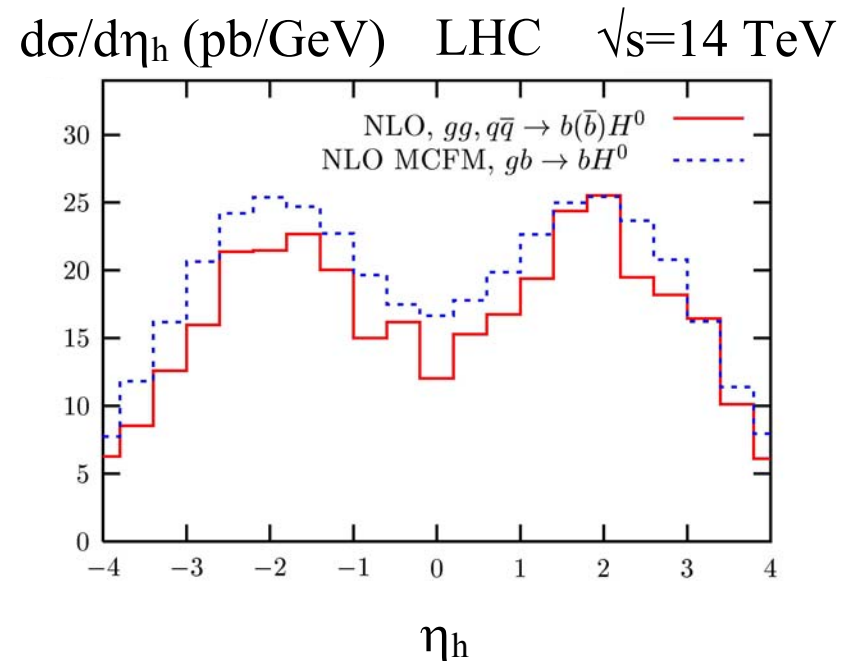
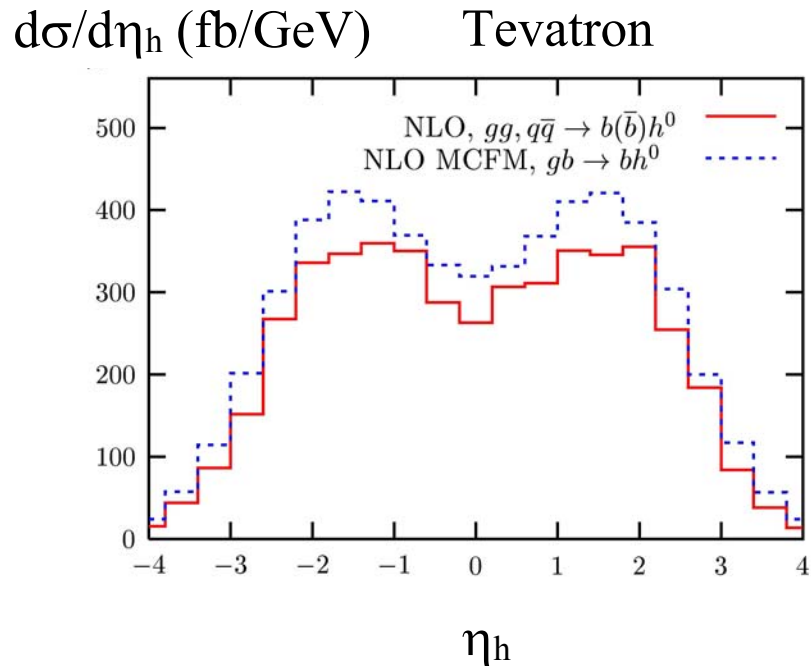


Consistent results for  
total cross sections



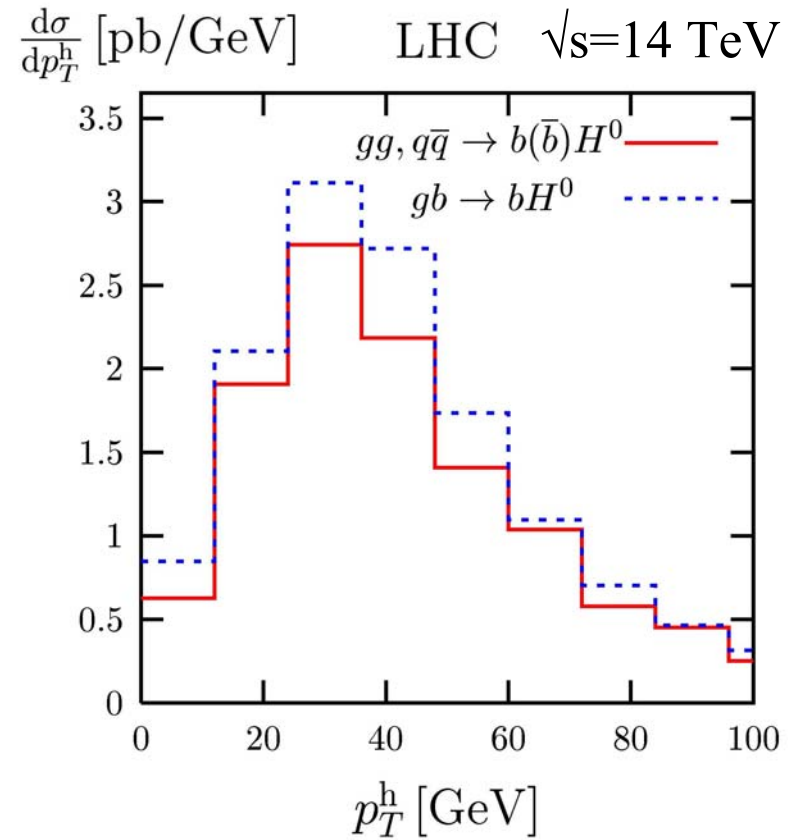
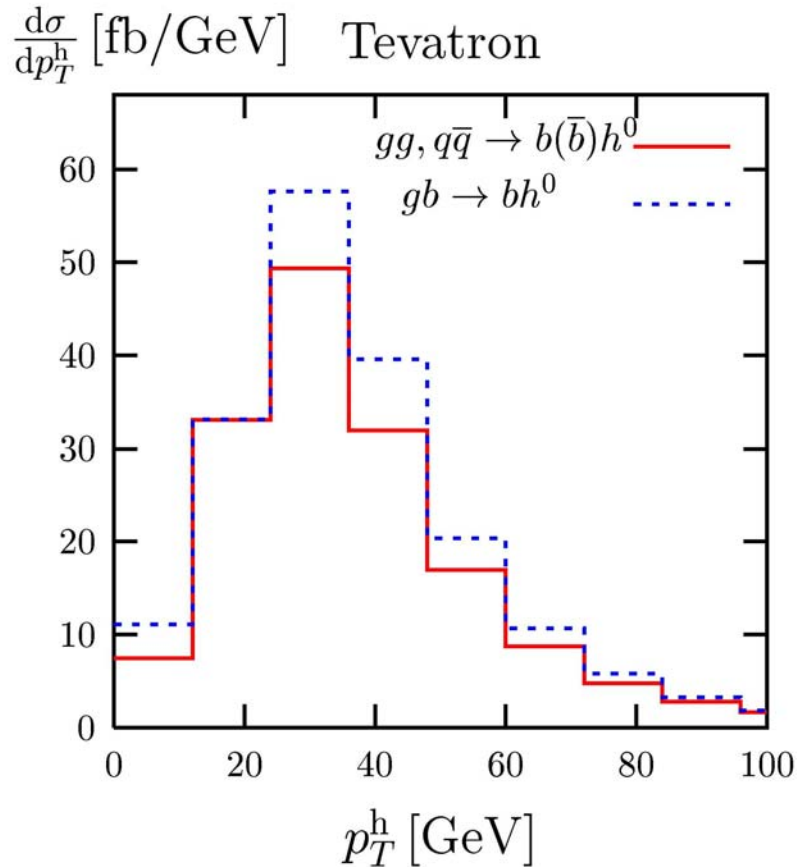
# Compare Distributions: Single b Tag

- 4FNS vs 5FNS: Important differences



MSSM with  $M_h=120$  GeV,  $\tan \beta=40$

# Compare distributions: Single b tag



MSSM with  $M_h=120$  GeV,  $\tan \beta=40$

# Calculate SUSY QCD Corrections to $bg \rightarrow bh$

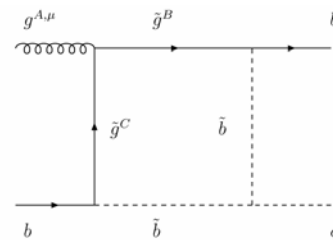
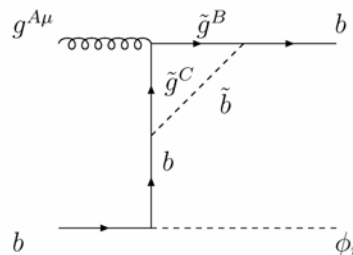
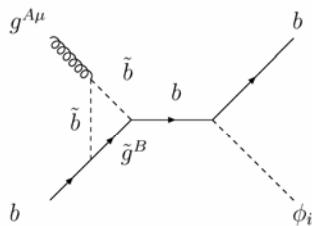
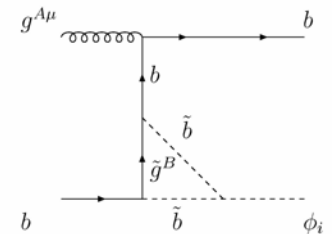
- Approach 1: Improved Born Approximation ( $\Delta m_b$ )

$$g_{hbb} \equiv \frac{m_b}{v_{SM}} \left( \frac{1}{1 + \Delta m_b} \right) \left( -\frac{\sin \alpha}{\cos \beta} \right) \left( 1 - \frac{\Delta m_b}{\tan \beta \tan \alpha} \right)$$

$$\sigma_{IBA} = \left( \frac{g_{hbb}}{g_{hbb}^{SM}} \right)^2 \sigma_{LO}$$

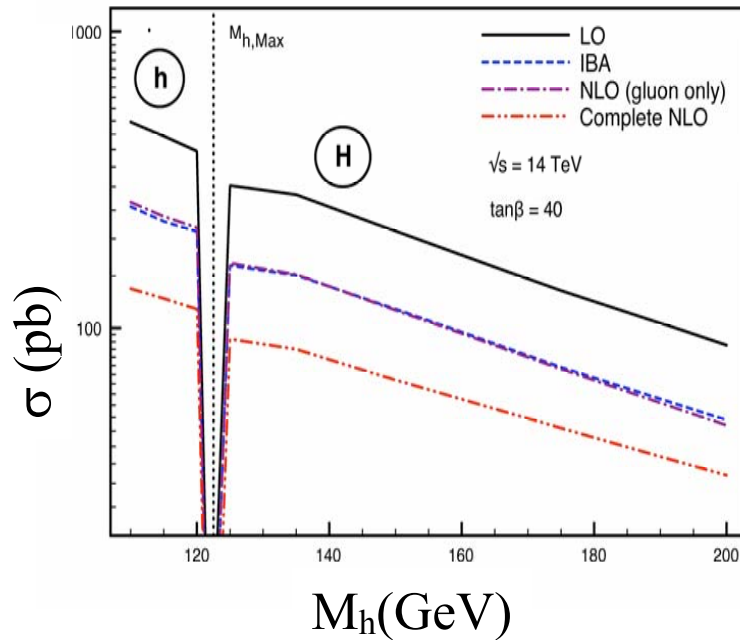
- Approach 2:  $O(\alpha_s^2)$  NLO calculation

- Use  $g_{hbb}$  as above, so subtract off double counting
- Include all contributions from squark/gluino loops

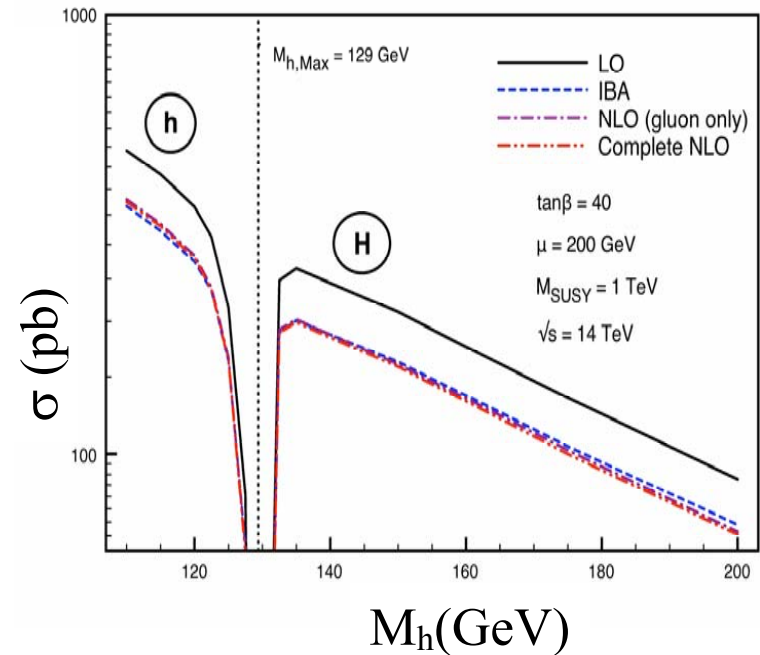


Many contributions  
not included in IBA

# Non-Decoupling of SQCD for Light SUSY ( $pp \rightarrow bH$ )



$$\tilde{m}_g = \tilde{m}_b = 250 \text{ GeV}$$

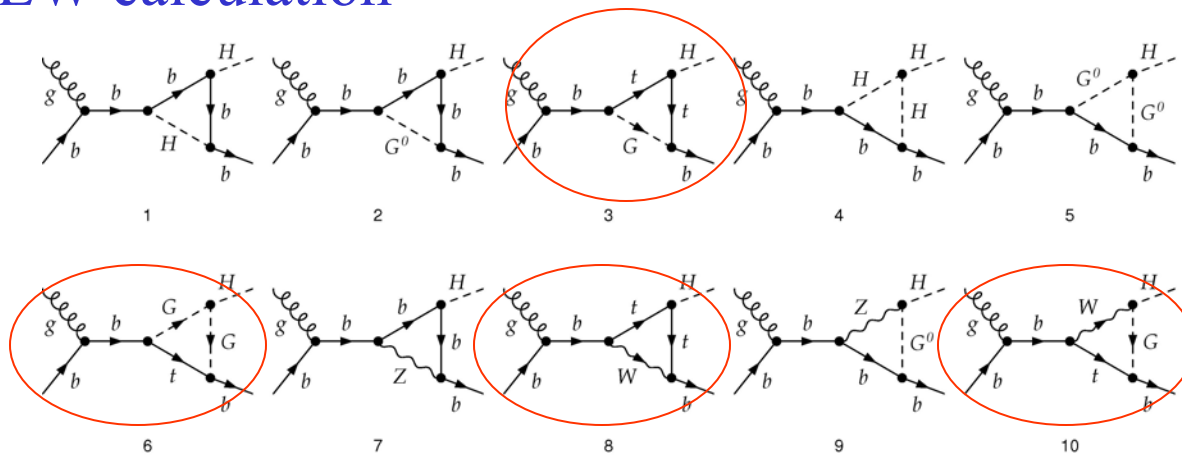


$$\tilde{m}_g = \tilde{m}_b = 1 \text{ TeV}$$

Improved Born Approximation fails for light SUSY particles

# Do Electroweak Corrections Matter?

- Lowest order rate for  $bg \rightarrow bh$  vanishes for  $m_b=0$
- At 1-loop, there are diagrams which do NOT vanish in  $m_b=0$  limit
- Full EW calculation

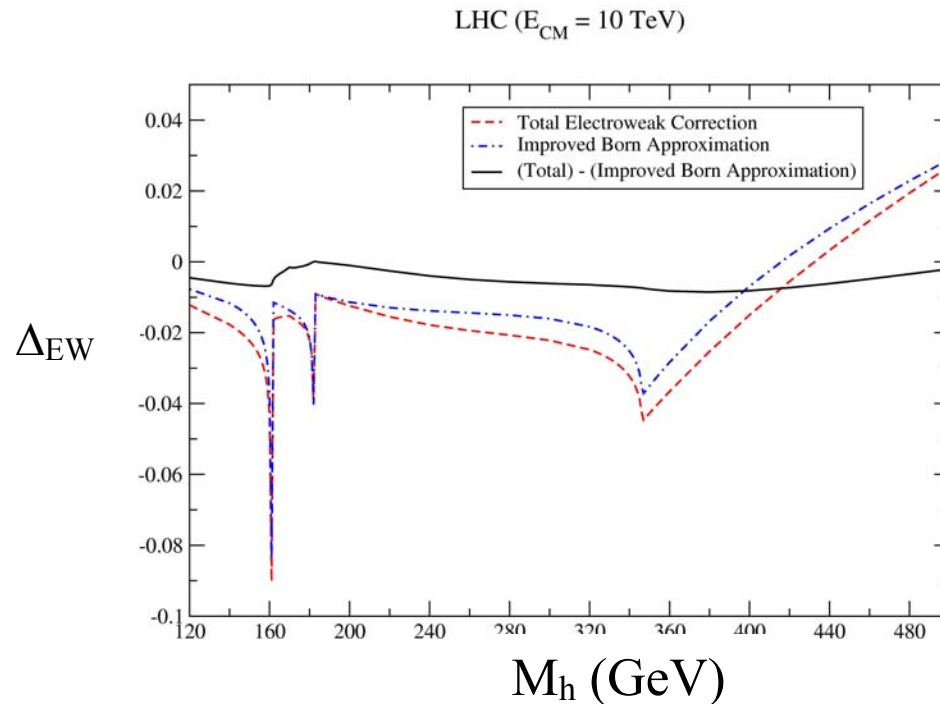


Plus many more diagrams.....

# EW Corrections to $pp \rightarrow bh$

$$\sigma(pp \rightarrow bH) = \sigma_0 \left( 1 + \Delta_{QCD} + \Delta_{SQCD} + \Delta_{EW} \right)$$

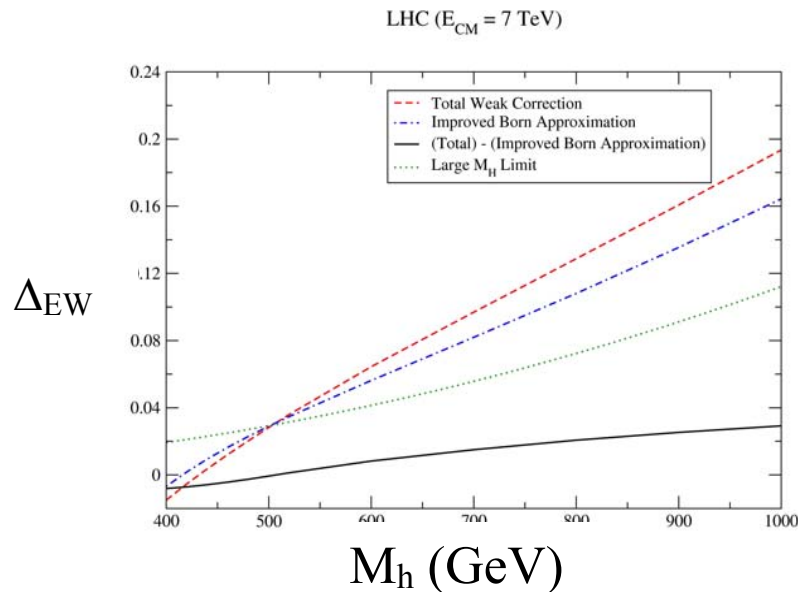
Improved Born  
Approximation  
captures weak  
corrections  
accurately



# EW corrections in large $M_h$ limit

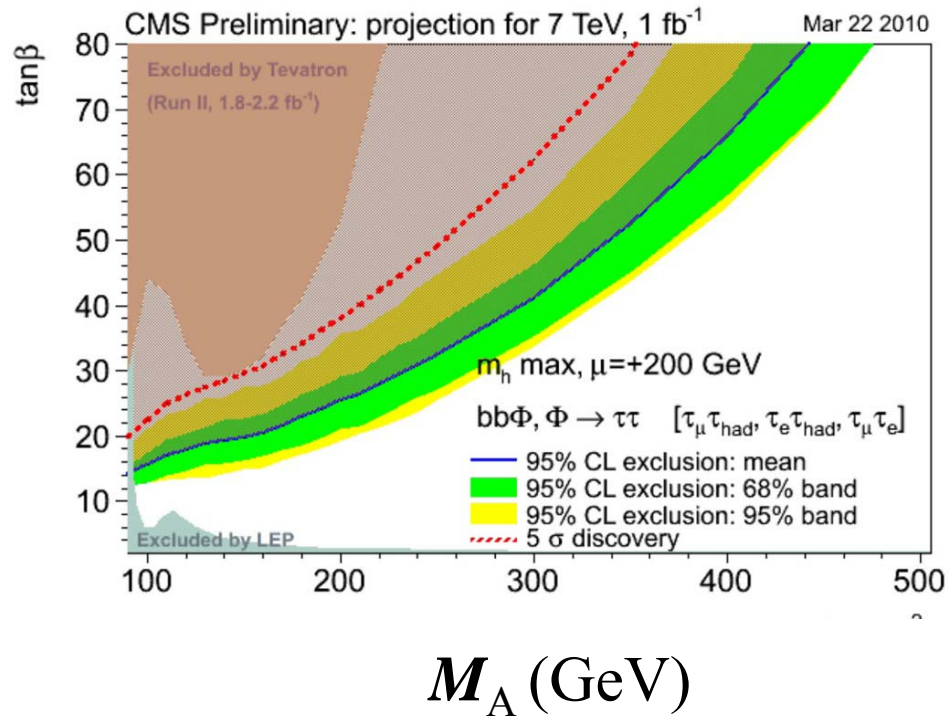
- Dominant contributions from  $\overline{b}b h$  vertex
  - No contributions which grow with  $M_h$  from triangle or box diagrams

$$\sigma(bg \rightarrow bh) \approx \sigma_0 \left( 1 + \frac{M_h^2}{32\pi v^2} [13 - 2\pi\sqrt{3}] \right)$$



- Need  $\log(M_h)$  pieces to reproduce full calculation
- Corrections  $O(18\%)$  for  $M_h \sim 1 \text{ TeV}$

# LHC Expectations



QCD and theory uncertainties will change this!



# Conclusions

- Compatible answers in 4FNS and 5FNS for total cross sections
  - Distributions in single b tag case slightly different
- EW corrections important at large  $M_h$ 
  - EW corrections for both 0 and 1 b tag can be included with effective Lagrangian
- SUSY QCD corrections can be important for light SUSY
  - For heavy SUSY can include SQCD in effective Lagrangian for single b tag
  - Effective Lagrangian works for all SUSY masses for 0 b tag
- Uncertainties from scheme dependence, PDFs, scale uncertainty significant